

**Comparison between the operational observation operator and the new canopy observation operator within the EKF off-line soil analysis scheme**

R. Hamdi

# 1. Jacobien of canopy observation operator

As a first experiment, the control vector  $x$  contains three prognostic variables of the ISBA-2L model: the root soil water content  $WG_2$ , the surface temperature  $TG_1$ , and the deep soil temperature  $TG_2$ . The observation vector contains the screen level temperature  $T_{2m}$  and relative humidity  $HU_{2m}$ . In this study, two observation operator are examined: (i) the vertical interpolation from the surface as computed from the ISBA-2L scheme to the observations level following the formulation of Geleyn (1988), (ii) the prognostic 2m values calculated with the new surface boundary layer scheme developed by Masson and Seity (2009) (Canopy scheme).

First, as suggested by Mahfouf et al. (2009), the elements of the Jacobian matrix are calculated using positive and negative perturbations which are set to  $10^{-4}$  for  $w_2$  and  $10^{-5}$  for  $T_s$  and  $T_2$ . The Jacobian of  $T_{2m}$  with respect to  $T_s$  is presented in Figure 1, corresponding to the four 6-h assimilation window examined on the 2 May 2009.

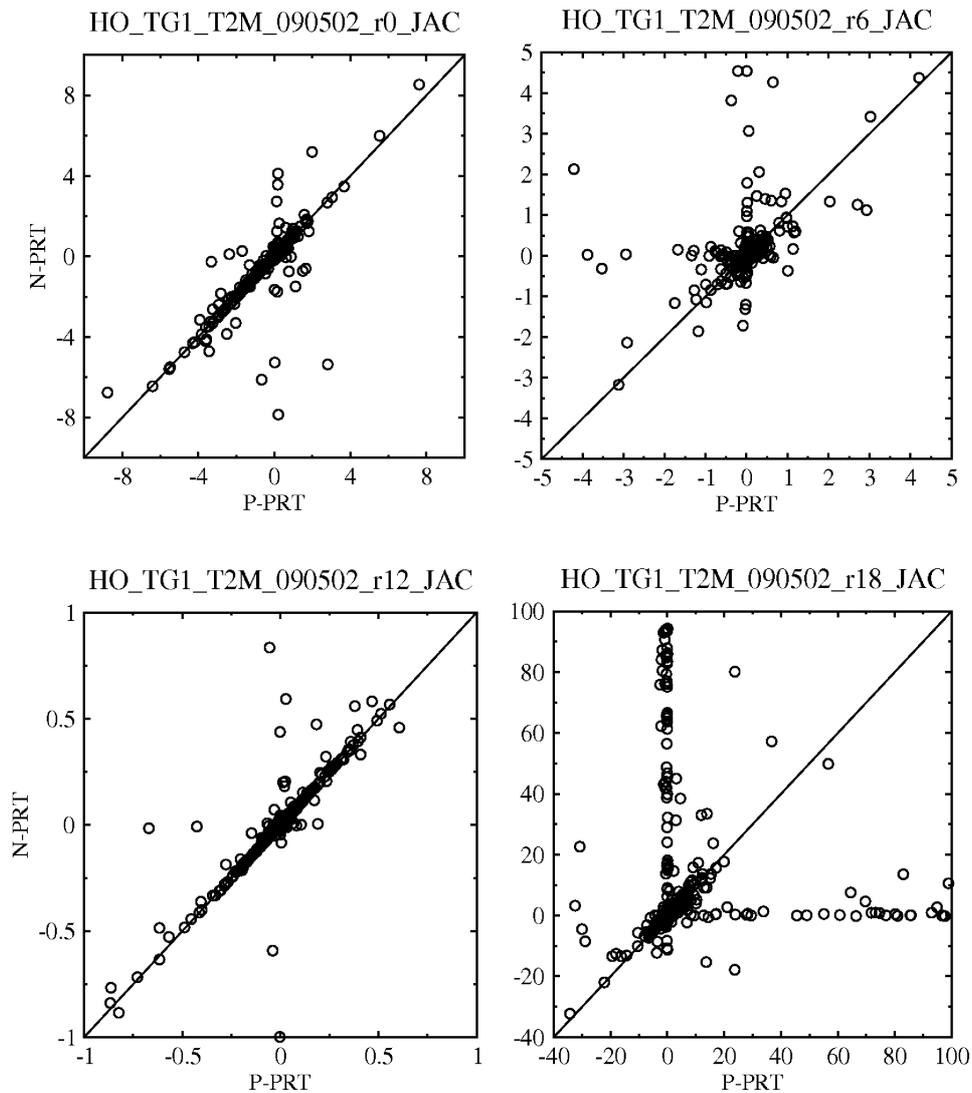


Figure 1.

Examination of the diurnal cycle reveals that the largest Jacobian are obtained for the night time (1800—0000) assimilation window. However, for this period, there are a number of points along the zero x (y) axis, indicating that in these instances there was no sensitivity to the negative (positive) perturbations, while the positive (negative) perturbations produced Jacobians with significant values. The locations of these points are mapped in Figure 2. At these points the perturbations are not small enough to reproduce the tangent-linear behavior of the observation operator. In fact, during the night the positive (or negative) perturbation of the surface temperature changes the stability regime of these locations and the validity of the linear regime breaks down. The same result is found for the the Jacobian of  $HU_{2m}$  with respect to  $T_s$  (see Figure 3).

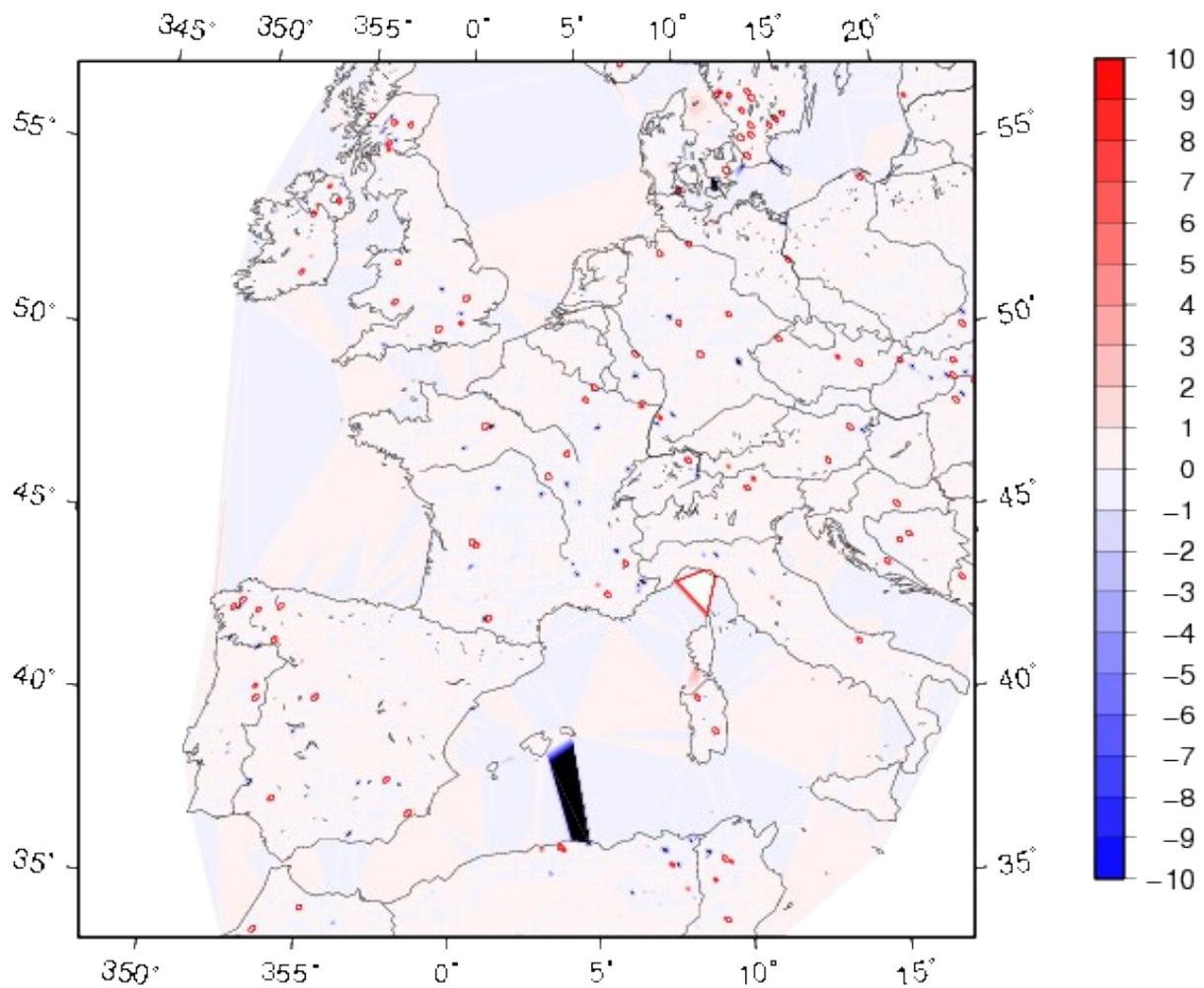


Figure 2.

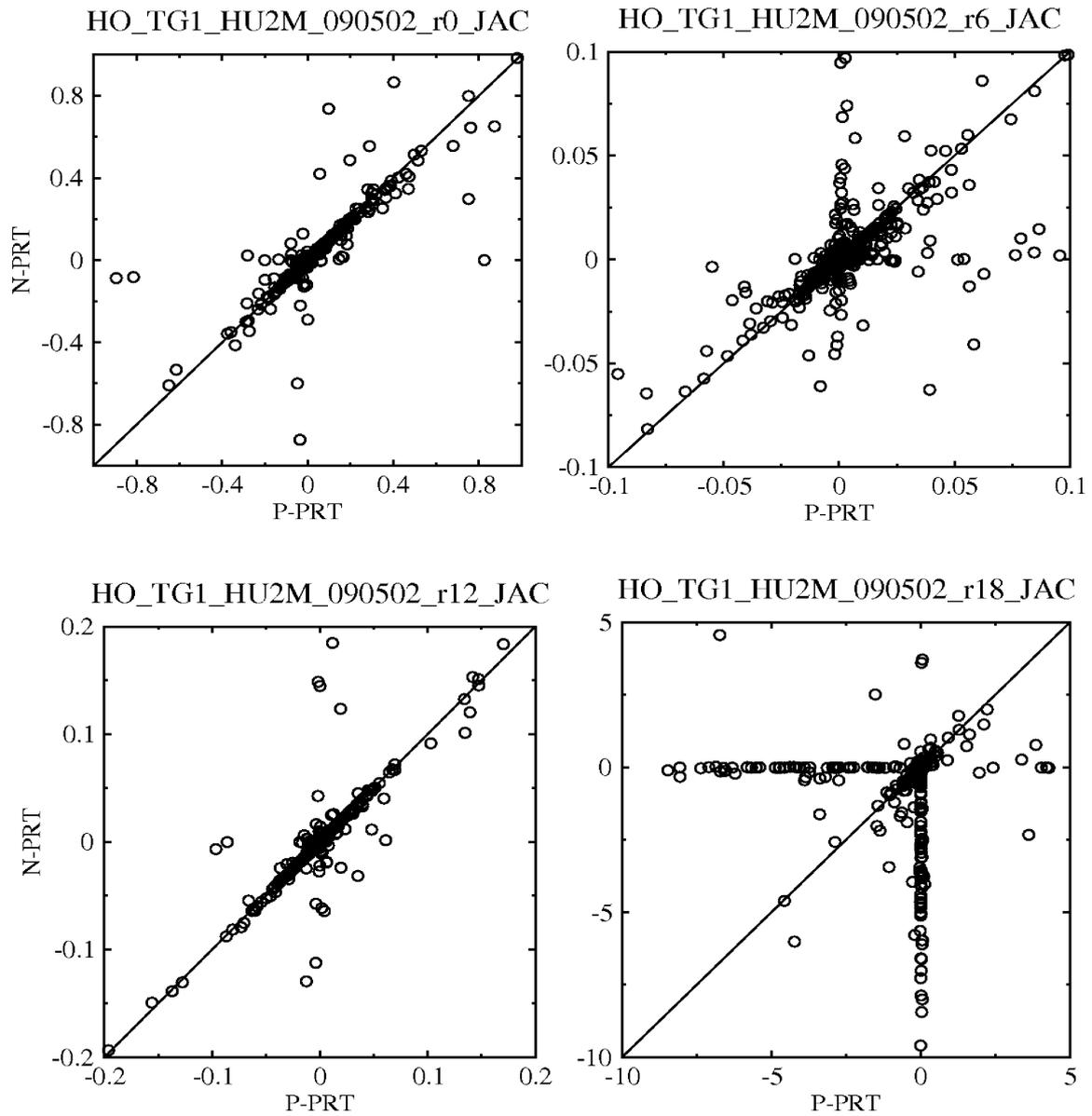


Figure 3.

A new experiment is performed using smaller perturbation for temperature ( $10^{-6}$  instead of  $10^{-5}$ ) and the same perturbation for the volumetric water content ( $10^{-4}$ ), the control vector  $x$  contains now the four prognostic variables of the ISBA-2L model:  $WG_2$ ,  $WG_1$ ,  $TG_1$ , and  $TG_2$ . The new Jacobian of  $T_{2m}$  and  $HU_{2m}$  with respect to  $TG_1$  is plotted in Figure 4. Almost all of the points are aligned along the one-to-one diagonal indicating that the finite difference estimates are now within the linear regime of the observation operator.

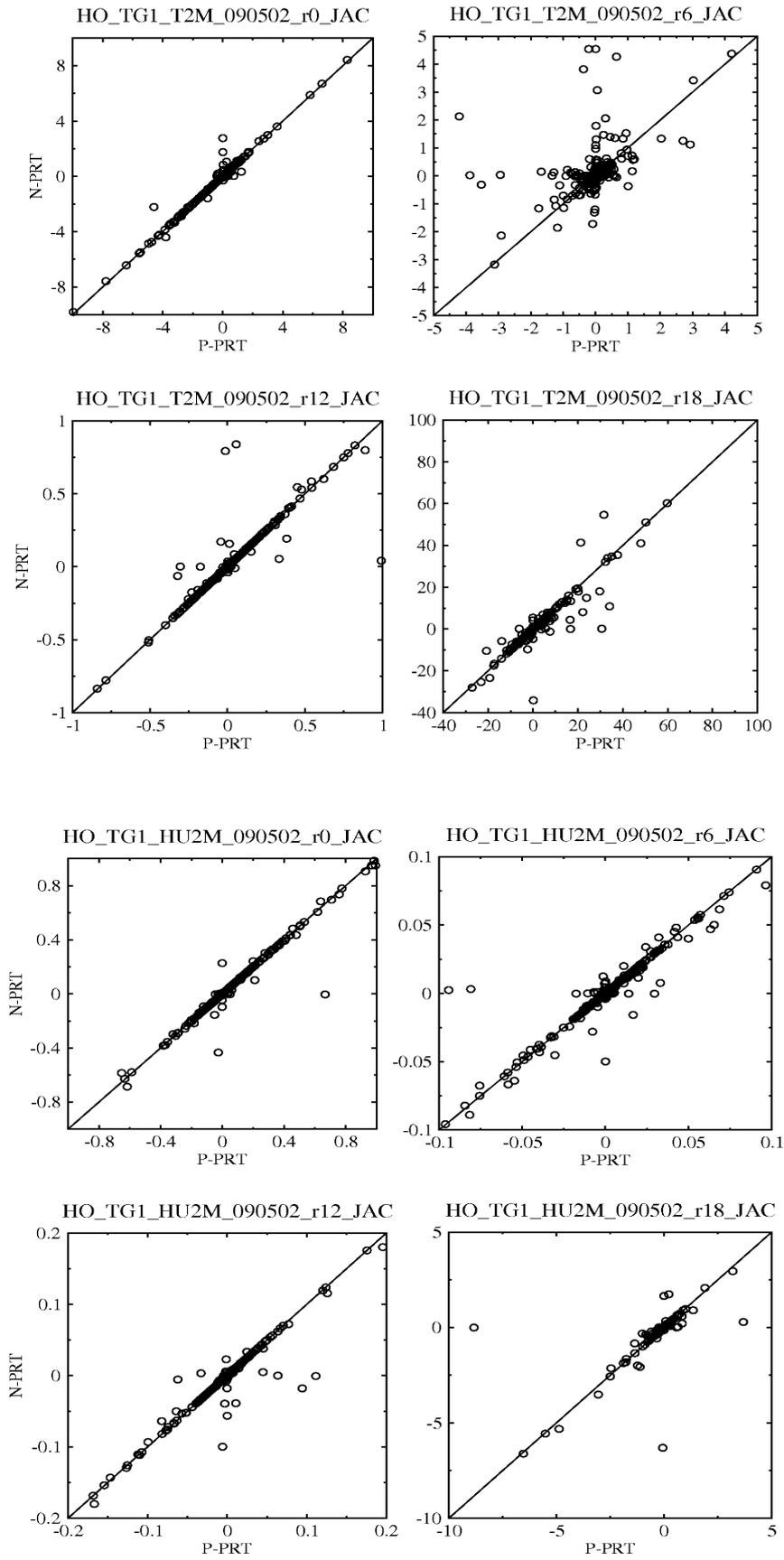


Figure 4.

## 2. Canopy observation operator & Geleyn observation operator

Since the Jacobians for the screen level variables with respect to  $WG_1$  and  $TG_1$  are an order of magnitude lower than those for  $WG_2$  and  $TG_2$  the comparison between the operational observation operator (based on the Geleyn's method) and the canopy observation operator will be done only for those two control variables. Figure 5 compares the Jacobians of  $T_{2m}$  with respect to  $TG_2$  corresponding to the four 6-h assimilation window.

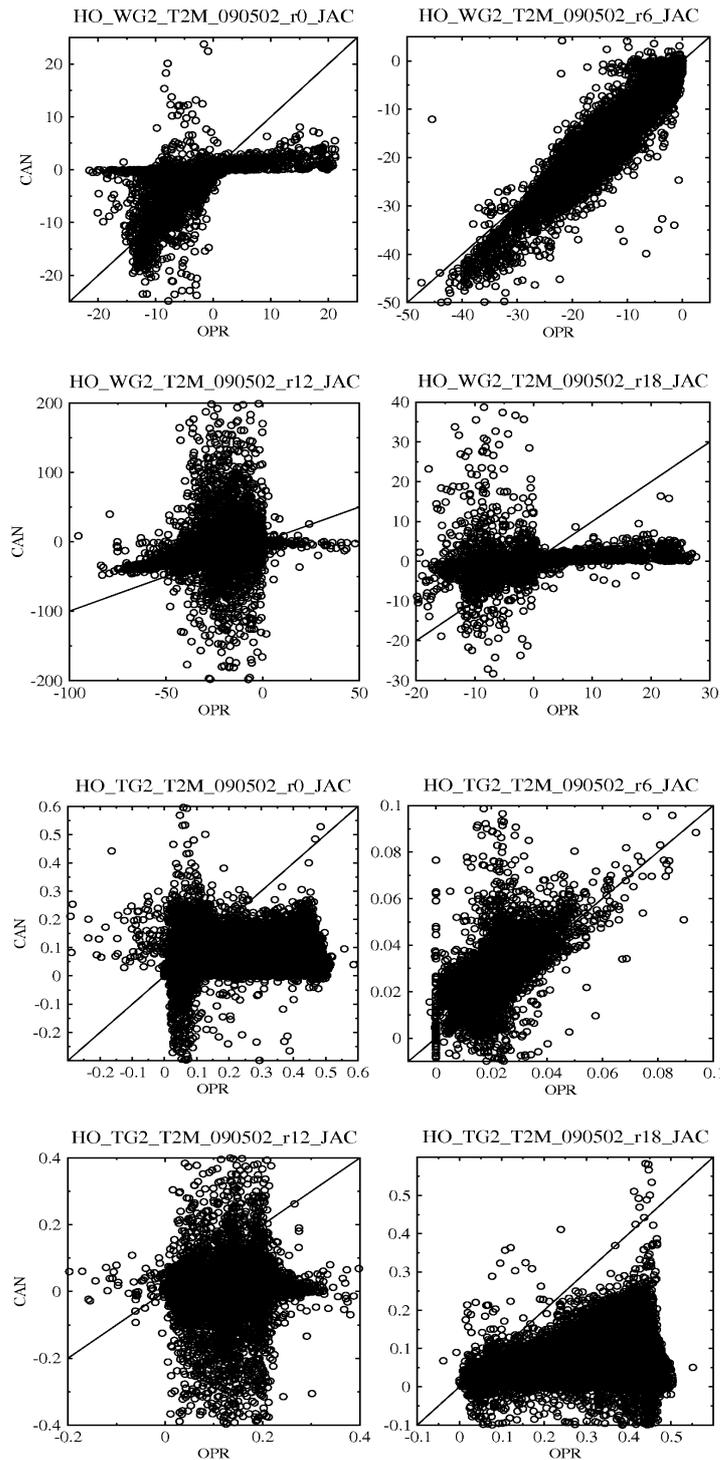


Figure 5.

It seems that the sensitivity of  $T_{2m}$  with respect to deep soil temperature (deep soil moisture) is lower (larger) with the canopy scheme especially during nighttime (daytime) where the Jacobians have their largest values. The difference between the Jacobians of  $T_{2m}$  with respect to  $WG_2$  calculated with the operational and the new canopy observation operator for the period 1200 1800 is plotted in Figure 6.

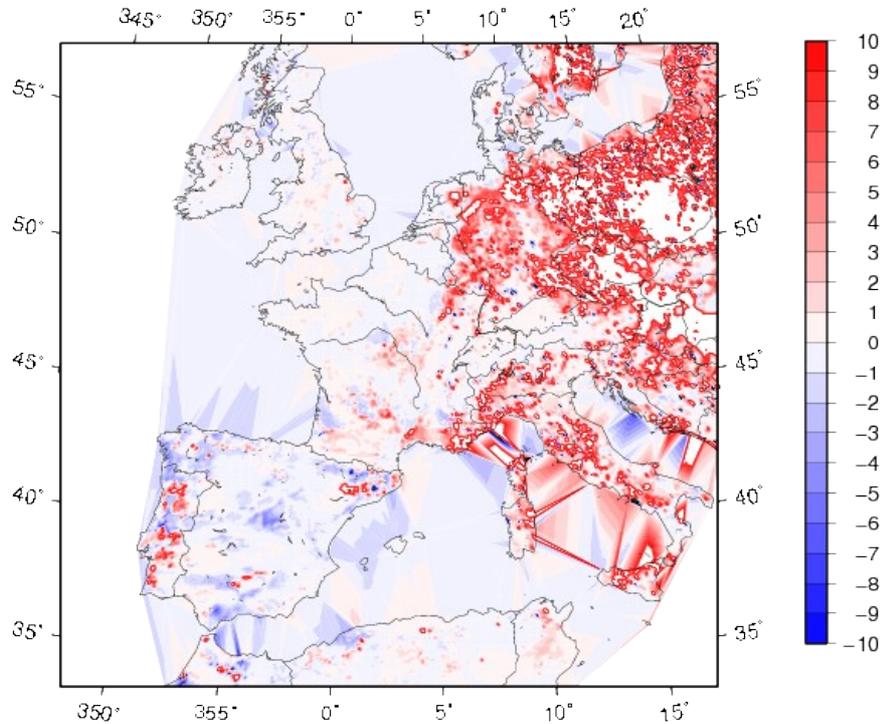


Figure 6.

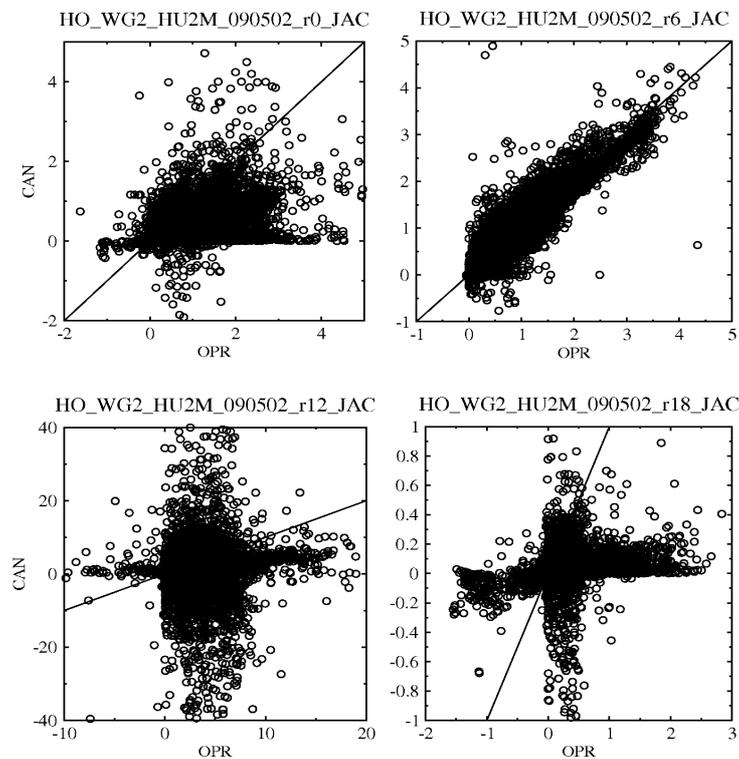
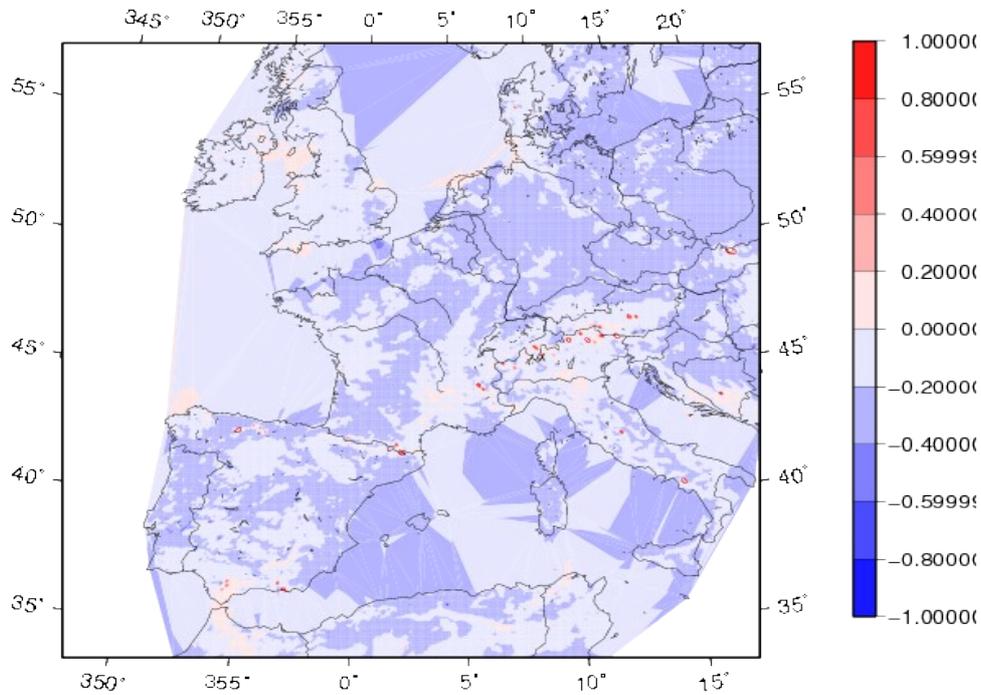


Figure 7.

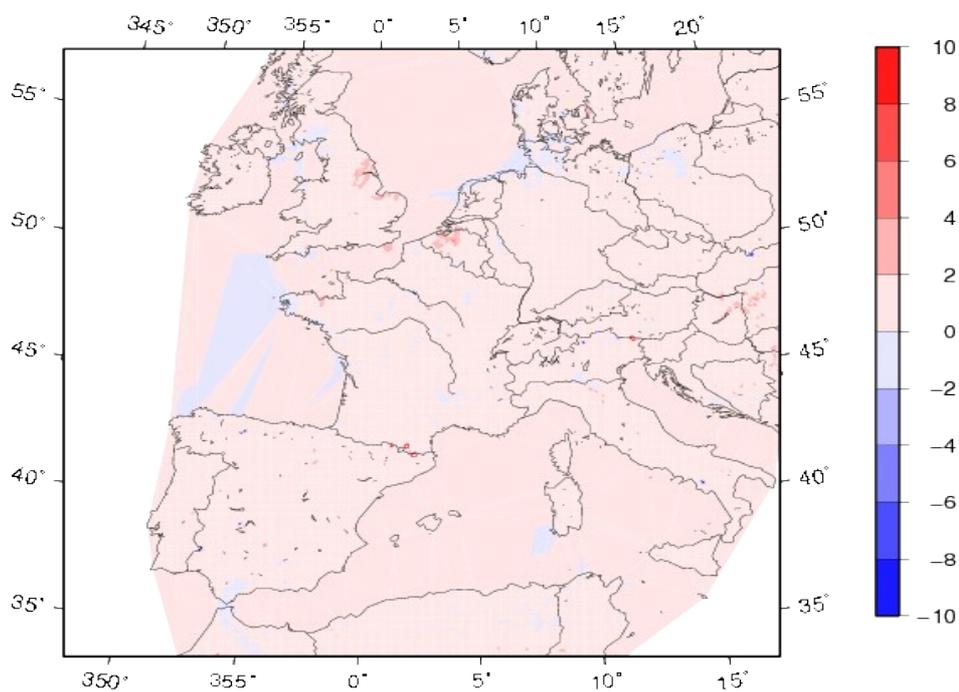
### 3. Kalman Gain Matrix

Figure 8 compares the Kalman gain matrix elements difference between CAN and OPR: (i)  $TG_2$  increments with respect to  $T_{2m}$  innovations, (ii)  $TG_2$  increments with respect to  $HU_{2m}$  on the 2 May at 1800.

(I)  $TG_2$  with respect to  $T_{2m}$

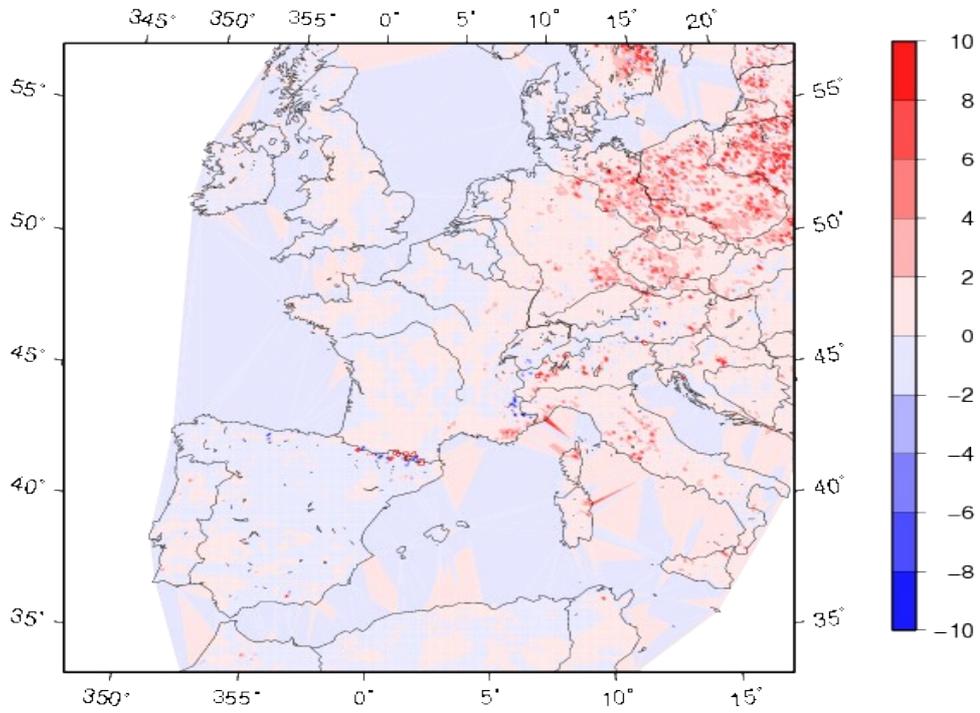


(ii)  $TG_2$  with respect to  $HU_{2m}$

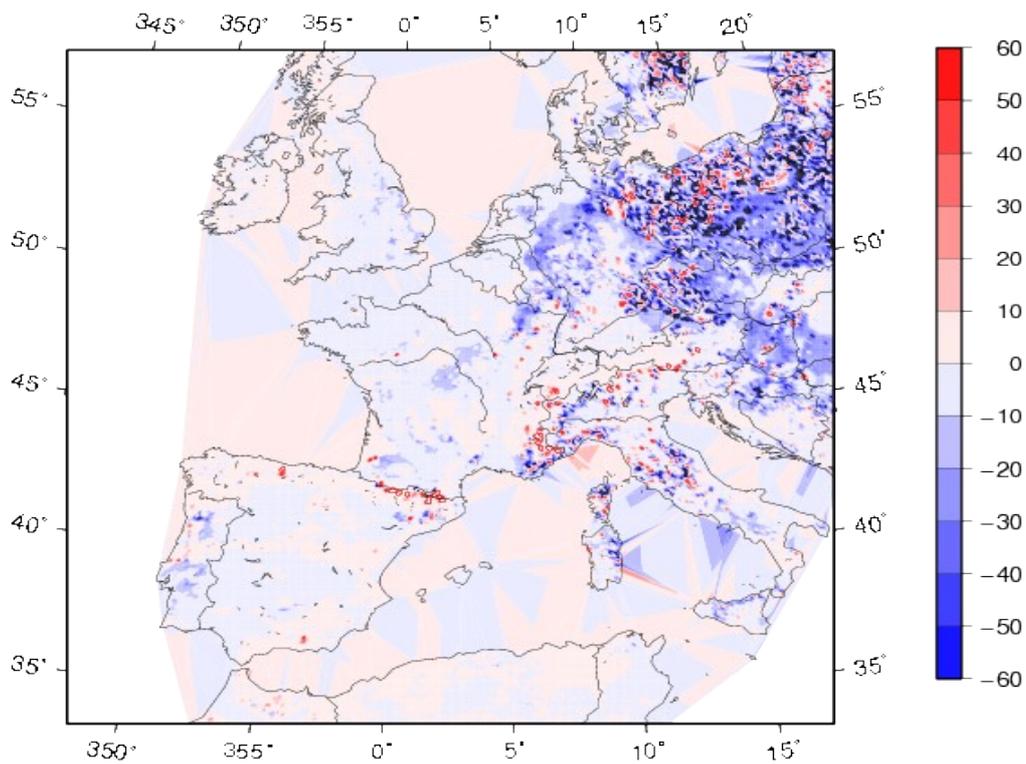


The link between screen level innovation and soil moisture correction in the root zone is plotted in Figure 8. The coefficients are multiplied by the soil depth on the 2 May at 1200.

(I)  $WG_2$  with respect to  $T_{2m}$



(ii)  $WG_2$  with respect to  $HU_{2m}$



## 4. Screen level analysis

The difference between OPR and CAN of the soil moisture increments in the root zone  $WG_2$  on 2 May at 1200.

